

## U.G. 3rd Semester Examination - 2022

**PHYSICS**

[HONOURS]

Generic Elective Course (GE)

Course Code : PHY-H-GE-T-01&amp;03

(Electricity and Magnetism)

Full Marks : 40

Time :  $2\frac{1}{2}$  Hours*The figures in the right-hand margin indicate marks.**Candidates are required to give their answers in their own words as far as practicable.***Answer all the questions from Selected Option.****OPTION-A****PHY-H-GE-T-01**

(Electricity and Magnetism)

**GROUP-A**

1. Answer any **five** questions:  $2 \times 5 = 10$
- Find the projection of the vector  $\vec{A} = \hat{i} - 2\hat{j} + \hat{k}$  on the vector  $\vec{B} = 4\hat{i} - 4\hat{j} + 7\hat{k}$ .
  - Write the differential form of Gauss's law.
  - Write the Ampere's Circuital law.
  - Write the Faraday's laws of electromagnetic induction.

*[Turn over]*



- e) Define magnetic susceptibility and permeability. Write the relationship between them.
- f) Write the differences between paramagnetic and ferromagnetic material.
- g) Define polarization vector of a dielectric. What is its physical significance?
- h) Define Poynting vector? Mention its physical significance.

**GROUP-B**

2. Answer any two questions: 5×2=10
- a) Write the Gauss's theorem of electrostatics. Apply this theorem to calculate the electric field at a distance  $r$  ( $r > a$ ), due to a uniformly charged infinite cylinder of radius  $a$ . 2+3
  - b) Derive the expression of potential and electric field due to an electric dipole. Define displacement vector. 4+1
  - c) Write the Biot-Savart's law. Apply this law to find the magnetic field at any axial point of a circular coil carrying a current  $I$ . 2+3
  - d) Show that electrostatic field is conservative. What is magnetic vector potential? 3+2



### GROUP-C

3. Answer any two questions:  $10 \times 2 = 20$

- a) Write down the relation between B, H and M. What is ferromagnetism? Explain the term 'hysteresis of a magnetic material'. Calculate the mutual force between two straight parallel conductors. each of length 1 metre in air 2.5 cm apart, when the current in each conductor is 250 Amp. Show that the energy expended in establishing a current 'I' in a coil of self inductance  $L$  is  $\frac{1}{2}LI^2$ .  $(1+1+2)+3+3$
- b) Using Gauss's theorem of electrostatics find the electric field at a distance  $r$  from the centre of a uniformly charged spherical shell for i)  $r > r_2$  and ii)  $r \leq r_1$ , Where ' $r_1$ ' and ' $r_2$ ' are the inner and outer radius respectively. Write the Gauss's theorem in dielectrics. Derive an expression of capacitance of a cylindrical capacitor whose inner and outer radii are 'a' and 'b' respectively.  $4+2+4$
- c) An electron moves in a circular orbit  $0.51 \text{ \AA}$  around nucleus at a frequency of  $6.8 \times 10^{15} \text{ Hz}$ . Find the magnetic induction at the nucleus and the equivalent magnetic moment.

Starting from the expression of magnetic vector

potential  $\vec{A} = \frac{\mu_0 I}{4\pi} \int \frac{d\vec{i}}{r}$  obtain the expression

$\vec{B} = \frac{\mu_0 I}{4\pi} \int \frac{d\vec{i} \times \vec{r}}{r^2}$ , where  $\vec{B} = \vec{\nabla} \times \vec{A}$ . Which law

does this expression represent?

If  $\vec{F} = 4xz\vec{i} - y^2\vec{j} + yz\vec{k}$ , evaluate  $\iint \vec{F} \cdot \vec{n} dS$ ,

where  $S$  is the surface of a cube bounded by

$x = 0, x = 1, y = 0, y = 1, z = 0, z = 1$ .

3+4+3

- d) Derive an expression of capacitance of a Parallel plate capacitor completely filled with a composite dielectric. Write the equation of continuity. Explain the concept of Displacement current? Derive the expression of velocity of electromagnetic wave using Maxwell's equations. 3+(2+2)+3



**OPTION-B**

**Course Code : PHY-H-GE-T-03**

**(Mechanics)**

**GROUP-A**

1. Answer any **five** questions:  $2 \times 5 = 10$
- a) Show that under Galilean transformation, acceleration of a particle remains invariant.
  - b) State and prove the work energy theorem.
  - c) Define radius of gyration for a rigid body rotating about a specified axis.
  - d) What is Poisson's ratio of a rigid body.
  - e) Determine the dimension of the coefficient of viscosity of a liquid .
  - f) Show that the field intensity is perpendicular to the displacement vector in an equipotential surface.
  - g) Write down the postulates of special theory of relativity.
  - h) Define Coriolis force with a vector diagram.

### GROUP-B

2. Answer any two questions:  $5 \times 2 = 10$

a) i) Find the general solution of the

differential equation  $\frac{d^2y}{dx^2} - 4\frac{dy}{dx} + 5y = 0$

ii) Solve:  $ydx - xdy - 3x^2y^2e^{x^3}dx = 0$   $3+2$

b) A body of mass  $m$  falling from a height  $h$  on a flywheel with radius  $R$ . Show that the linear

acceleration  $a$  of the mass is,  $a = \frac{g}{\left(1 + \frac{1}{mr^2}\right)}$

(where  $g$  is gravitational acceleration)  $5$

c) Establish the relation among Young's modulus ( $Y$ ), Rigidity modulus ( $\eta$ ) and Poisson's ( $\sigma$ ) of a rigid body.  $5$

d) Calculate the period of a second pendulum measured by an observer travelling at 80% of the speed of light.  $5$

### GROUP-C

3. Answer any two questions:  $10 \times 2 = 20$

a) i) Considering the differential equation of an orbit derive Newton's law of gravitation.



ii) Show that the angular momentum of a planet revolving round the sun remains constant. 5+5

b) The differential equation for a one dimensional damped harmonic oscillator is given by

$$m \frac{d^2x}{dt^2} + K \frac{dx}{dt} + Sx = 0$$

Explain the significance of each term in the equation. Solve the equation for overdamped condition. 2+8

c) i) Prove that  $\vec{A} \times (\vec{B} \times \vec{C}) = \vec{B}(\vec{A} \cdot \vec{C}) - \vec{C}(\vec{A} \cdot \vec{B})$

ii) Prove that central force is conservative.

iii) Show that areal velocity is constant for planetary motion. 4+4+2

d) i) Reduce a two body system to an equivalent one body system.

ii) Three particles of masses 4Kg, 3Kg, and 2Kg are at the points (2, 0, -1), (1, 1, 3) and (3, -1, 0) respectively. Find the coordinates of the centre of mass.

iii) Write down the necessary and sufficient condition of a first order differential equation to be exact. 5+3+2