

## Determination of The Order Of Reaction

(i) **The Differential Method:** This method was suggested by van't Hoff and therefore it is sometimes called as van't Hoff method. According to this method the rate of a reaction of nth order is proportional to the nth power of concentration.

$$-d[A]/dt = k[A]^n$$

where [A] is the concentration at any instant. In two experiments with initial concentration  $[A]_1$  and  $[A]_2$

$$-d[A]_1/dt = k[A]_1^n$$

$$-d[A]_2/dt = k[A]_2^n$$

Taking logarithms, we get  $\log\{-d[A]_1/dt\} = \log k + n \log[A]_1$

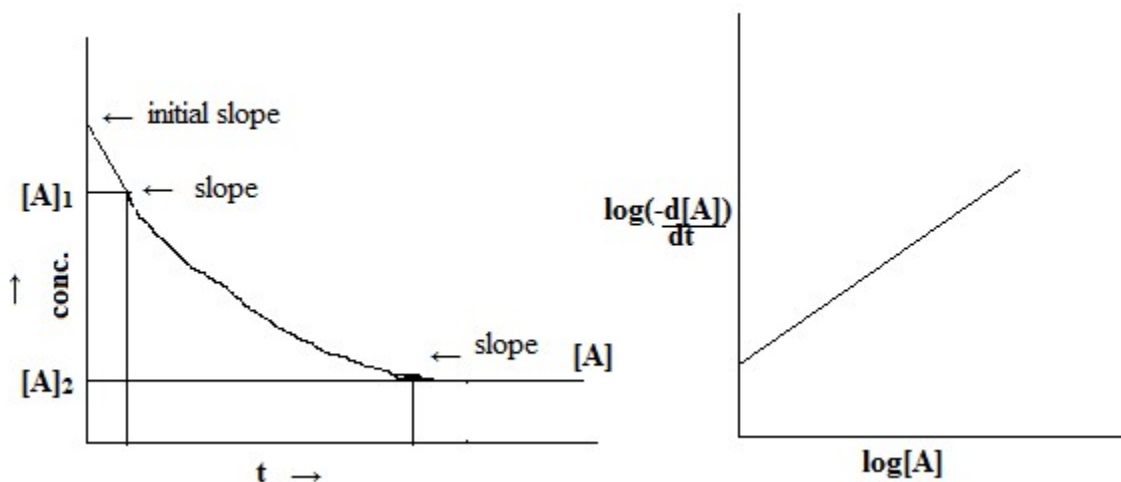
and  $\log\{-d[A]_2/dt\} = \log k + n \log[A]_2$

Subtracting, we have,

$$n = \frac{\log\{-d[A]_1/dt\} - \log\{-d[A]_2/dt\}}{\log[A]_1 - \log[A]_2}$$

An approximation method used to determine  $-d[A]/dt$  is as follows: This rate of change in A over an appreciable time interval, i.e.,  $-\Delta A/\Delta t$  is measured and assumed to be  $-d[A]/dt$  corresponding to the mean value of A in the interval considered.

A better method is to plot concentration versus time for two experiments with different initial concentration. The slope ( $-d[A]/dt$ ) at a given interval is measured by drawing tangents. Using these values of slopes ( $-d[A]/dt$ ) in the above equation, n is determined.



**Figure 6: Plot of  $(-d[A]/dt)$  vs time and  $\log(-d[A]/dt)$  vs  $\log[A]$  for differential method**

**(ii) Half-Life method:** At the time at which half of the reactant disappear is the half-life period ( $t_{1/2}$ ). For a first order reaction this value is constant and is independent of the initial concentration of the reactant. For a second order reaction,  $t_{1/2}$  is inversely proportional to the initial concentration of the reactant. In general, for a reaction of  $n$ th order,  $t_{1/2}$  is given by Eq(45), i.e.,

$$t_{1/2} \propto 1/a^{n-1}$$

where  $a$  is the initial concentration of the reactant and  $n$  is the order of the reaction. Suppose two different experiments are carried out with initial concentrations as  $a_1$  and  $a_2$ , then their half-life periods  $(t_{1/2})_1$  and  $(t_{1/2})_2$  would be related as

$$(t_{1/2})_1 / (t_{1/2})_2 = (a_2/a_1)^{n-1}$$

$$(n-1)\log(a_2/a_1) = \log(t_{1/2})_1 / (t_{1/2})_2$$

$$n = 1 + \frac{\log(t_{1/2})_1 / (t_{1/2})_2}{\log(a_2/a_1)}$$

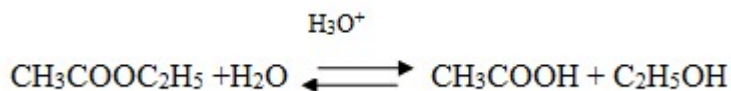
Hence  $n$  can be evaluated.

## Complications in Reaction Kinetics

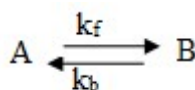
There are many reaction which are accompanied by side reactions in the addition to the main reaction. Such reactions do not take place in a single stage but occur in a number of well defined steps. In these cases the rate law is inconsistent with the stoichiometric equation for the reaction. The usual types of complications are:

- i) Reversible or opposing reaction
- ii) Parallel reactions
- iii) Consecutive reactions

**i) Reversible or opposing reaction:** In general it is assumed that the reactions are process in one direction only. If the products formed react to produce the reactants back, the reaction is said to be an **opposing** or a **reversible** reaction. In such instances, the ration of the reverse reaction increases as more and more of the products are formed and eventually the two rates viz., forward and reverse become equal; the overall rate is then zero. A well known example is the hydrolysis of ethyl acetate in aqueous solution



The simplest process is that of a reversible or opposing reaction where the reaction is 1<sup>st</sup> order in both the directions. The reactions considered are simple except this complication so that it may be written as



The reactant A changes to B with a specific rate  $k_f$  and B changes to A with a specific rate  $k_b$ . Let only A be present initially and let the initial concentration a gm moles/l. x gm moles/l be converted into B at time t, then the net rate of production of B is

$$dx/dt = k_f(a-x) - k_b x \dots\dots\dots (46)$$

Let  $x_e$  be the amount of B at equilibrium. Then

$$k_f(a-x_e) = k_b x_e$$

so,  $k_b = k_f(a-x_e)/x_e \dots\dots\dots (47)$

Putting eqn. (47) in (46)

$$dx/dt = k_f(a-x) - k_f(a-x_e)x/x_e \dots\dots\dots (48)$$

$$= k_f(x_e-x)a/x_e \dots\dots\dots (49)$$

$$\text{or, } dx/(x_e-x) = k_f a dt/x_e$$

Integrating

## Chemical Kinetics

$$-\ln(x_e - x) = k_f a t / x_e + I_c$$

When  $t=0$ ,  $x=0$ , Thus,  $I_c = -\ln x_e$ , consequently,  $\ln x_e / (x_e - x) = k_f a t / x_e$  .....(50)

So,

$$k_f = \frac{x_e}{a t} \ln \frac{x_e}{x_e - x}$$

From eq (47)

$$k_b = \frac{a - x_e}{a t} \ln \frac{x_e}{x_e - x} \dots\dots\dots (51)$$

Naturally,

$$k_f + k_b = \frac{1}{t} \ln \frac{x_e}{x_e - x} \dots\dots\dots (52)$$